Expressive Genetic Programming: Concepts and Applications

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Outline

- The Push programming language
- Types and control without syntax
- Evolving Push programs
- Understanding expressive program evolution
- Evolving program evolution

Push

- Programming language for programs that evolve
- Data flows via per-type stacks, not syntax
- Trivial syntax, rich data and control structures
- PushGP: GP system that evolves Push programs
- C++, Clojure, Common Lisp, Elixir, Java, Javascript, Python, Racket, Ruby, Scala, Scheme, Swift; **build your own in any language quickly**
- <http://pushlanguage.org>

Expressive

- Multiple types
- Arbitrary control
- Multiple tasks (use lexicase selection)
- Self reproduction/variation (optional)
- Flexibility, resilience, neutrality

The Push VM

integer_mult		True	
boolean_and	7	False	
(3 string_dup)	-20	True	"Hello"
integer_add	100	False	"Push"
			"Evolution!"
Exec	Integer	Boolean	String
			...

Push Execution

- Push the program onto the **exec** stack.
- While **exec** isn't empty and we haven't hit the step limit, pop and do the top:
 - If it's an instruction, execute it. (Insufficient arguments? Do nothing.)
 - If it's a literal, push it onto the appropriate stack.
 - If it's a list, push its elements back onto the **exec** stack one at a time.

Example Execution

		True		
integer_mult		False		
boolean_and	7	True	"Hello"	
(3 string_dup)	-20	True	"Push"	
integer_add	100	False	"Evolution!"	
Exec	Integer	Boolean	String	...

		True		
		False		
boolean_and		True	"Hello"	
(3 string_dup)	-140	True	"Push"	
integer_add	100	False	"Evolution!"	
Exec	Integer	Boolean	String	...

		False		
		True	"Hello"	
(3 string_dup)	-140	True	"Push"	
integer_add	100	False	"Evolution!"	
Exec	Integer	Boolean	String	...

		False		
3		True	"Hello"	
string_dup	-140	True	"Push"	
integer_add	100	False	"Evolution!"	
Exec	Integer	Boolean	String	...

		False	
	3	True	"Hello"
string_dup	-140	True	"Push"
integer_add	100	False	"Evolution!"
Exec	Integer	Boolean	String
			...

		False	"Hello"
	3	True	"Hello"
	-140	True	"Push"
integer_add	100	False	"Evolution!"
Exec	Integer	Boolean	String
			...

		False	"Hello"
		True	"Hello"
	-137	True	"Push"
	100	False	"Evolution!"
Exec	Integer	Boolean	String
			...

(1 2 integer_add)			
Exec	Integer	Boolean	String
			...

Full Program

1
2
integer_add

Exec	Integer	Boolean	String	...
-------------	----------------	----------------	---------------	------------

2
integer_add

1

Exec	Integer	Boolean	String	...
-------------	----------------	----------------	---------------	------------

integer_add 2
1

Exec	Integer	Boolean	String	...
-------------	----------------	----------------	---------------	------------

3

Exec	Integer	Boolean	String	...
-------------	----------------	----------------	---------------	------------

```
(1 2 integer_add)
```

leaves 3 on the integer stack

```
(True False boolean_or boolean_not)
```

leaves False on the boolean stack

```
(3 5 integer_lte)
```

leaves True on the boolean stack

```
(3 5 integer_lte exec_if (1 "yes") (2 "no"))
```

leaves "yes" on string, 1 on integer

For Most Types

- <type>_dup
- <type>_empty
- <type>_eq
- <type>_flush
- <type>_pop
- <type>_rot
- <type>_shove
- <type>_stackdepth
- <type>_swap
- <type>_yank
- <type>_yankdup

Selected Integer Instructions

```
integer_add integer_dec integer_div  
integer_gt integer_fromstring integer_min  
integer_mult integer_rand
```

Selected Boolean Instructions

```
boolean_and boolean_xor boolean_frominteger
```

Selected String Instructions

```
string_concat string_contains string_length  
string_removechar string_replacechar
```

Exec (selected)

Conditionals:

```
exec_if exec_when
```

General loops:

```
exec_do*while
```

"For" loops:

```
exec_do*range exec_do*times
```

Looping over structures:

```
exec_do*vector_integer exec_string_iterate
```

Combinators:

```
exec_k exec_y exec_s
```

More

```
code atom code car print newline integer_sub integer_inc boolean_stackdepth return_exec pop vector_integer_eq autoconstructive_integer_rand boolean_pop
genome_close_inc string_fromchar vector_string_show zip_yankdup genome_new_vector_float_yankdup exec_yankdup vector_integer_show integer_yankdup string_flush
boolean_swap zip_empty exec_show vector_boolean_yank code_eq exec_y boolean_yank integer_eq genome_silence string_boolean code_contains string_contains
code_do_count vector_float_last genome_pop string_substring integer_mult code_length vector_integer_integer_dup boolean_or code_position boolean_empty zip_fromcode
print_vector_string vector_boolean_swap return_frominteger vector_float_pushall char_inhitegap code_cdr exec_do_vector_integer_rand
vector_string_replacefirst string_first vector_boolean_first exec_do_while exec_string_iterate string_indexofchar vector_float_replace integer_fromstring
code_list code_swap char_frominteger genome_gene_randomize vector_integer_emptyvector vector_string_eq vector_float_boolean exec_empty zip_end? exec_fromipnode
string_show vector_boolean_pushall zip_insert_left fromcode exec_rot vector_string_concat vector_float_indexof code_pop vector_string_subvec vector_integer_swap
code_subst char_pop return_string_pop zip_yank exec_dup vector_integer_boolean vector_float_rest vector_string_flush boolean_fromfloat code_fromziprights
float_glt boolean_float char_laddigit float_the exec_fromiproot vector_integer_empty print_code vector_string_stackdepth string_reverse exec_>
vector_integer_yank float_frominteger char_rot print_char vector_integer_stackdepth vector_boolean_concat boolean_xor integer_gte genome_yankdup
vector_float_show vector_integer_take code_quote string_replacefirst return_fromstring exec_fromziplefts vector_integer_yankdup boolean_show float_lt
vector_string_dup vector_string_occurrencesof vector_integer_replace zip_branch? vector_float_reverse float_not vector_float_subvec string_last print_boolean
boolean_rot vector_string_rest integer_div vector_float_remove integer_fromfloat integer_lte code_fromzipchildren environment_and vector_integer_rot integer_mod
string_concat vector_string_boolean genome_swap code_null exec_do_count vector_float_emptyvector vector_string_yankdup integer_rot float_yankdup
vector_string_rot zip_replace fromexec vector_string_take integer_add vector_integer_occurrencesof integer_show genome_dup return_code_pop char_swap integer_max
return_fromexec code_swap return_float_pop code_flush genome_yank zip_show vector_integer_flush vector_integer_subvec vector_boolean_indexof vector_float_pop
integer_string_remove vector_integer_contains zip_remove code_append vector_float_eq vector_integer_conj string_eq zip_leftmost code_yankdup code_rot
integer_stackdepth float_max vector_boolean_set zip_append_child fromexec zip_rest vector_float_conj zip_fromexec string_take zip_left zip_replace fromcode
char_stackdepth return_fromchar genome_eq vector_integer_replacefirst float_stackdepth code_fromiproot float_fromchar float_glt boolean_dup float_fromboolean
code_fromipnode genome_rot vector_float_replacefirst vector_boolean_conj vector_boolean_dup vector_integer_indexof vector_string_swap exec_eq string_emptystring
string_swap integer_yank exec_while float_empty print_vector_boolean integer_and exec_swap genome_rotate integer_fromchar vector_string_yank string_stackdepth
code_dorange string_replacechar char_atifromstring vector_integer_rest vector_boolean_length char_yank vector_float_empty code_fromfloat genome_parent2
return_fromcode string_pop float_eq vector_boolean_empty zip_insert_child fromexec vector_string_last string_nth code_do? return_zip_pop vector_string_pop
zip_rot vector_integer_nth exec_dorange exec_if char_show zip_down zip_insert_left fromexec code_frominteger vector_boolean_remove vector_integer_remove
vector_integer_last char_listiter genome_gene_dup vector_integer_concat print_integer code_pop boolean_eq float_glt return_fromfloat genome_gene_copy
string_occurrencesofchar string_replacefirstchar print_float_boolean_rand integer_flush float_show string_replace char_dup float_pop char_eq vector_float_nth
vector_string_conj integer_gt return_integer pop float_sub vector_integer_length vector_float_ses vector_string_indexof vector_boolean_rest code_dup
vector_boolean_show zip_eq float_min boolean_not float_mult float_fromstring genome_unsilence code_if vector_integer_pop vector_boolean_last exec_dortimes
zip_pop zip_rightmost float_dec vector_float_contains genome_gene_copy range environment_new exec_do_vector_string code_nthcdr string_empty char_empty exec_pop
vector_integer_ses autoconstructive_boolean_rand vector_float_rot string_yankdup exec_do_vector_float_string_removechar code_extract vector_string_replace
vector_float_first genome_parent return_tapepace char_flush vector_float_occurrencesof vector_string_emptyvector float_add code_stackdepth exec_s
zip_insert_right fromexec float_dup vector_string_nth zip_stackdepth vector_integer_reverse print_vector_integer char_fromfloat code_dortimes code_noop zip_swap
code_yank integer_lt vector_boolean_eq genome_stackdepth code_fromziplefts noop_open_paren string_containschar string_yank char_rand zip_flush vector_boolean_rot
float_swap exec_fromzipright vector_string_ses vector_boolean_flush exec_noop code_size vector_boolean_stackdepth vector_integer_pushall
vector_boolean_reverse integer_swap string_split vector_boolean_contains string_fromboolean return_boolean_pop vector_float_dup vector_boolean_replace
integer_dup vector_boolean_nth vector_string_length string_rest zip_insert_child fromcode float_tan string_rot string_rand exec_show string_pare to_chars
integer_pop integer_empty vector_float_flush vector_float_yank noop_delete_prev_paren_pair print_exec_zip_append_child fromcode genome_gene_delete code_empty
float_inc zip_right vector_float_length float_rand integer_dec string_contains return_fromboolean vector_float_concat vector_float_stackdepth
exec_do_vector_boolean vector_integer_first genome_show code_rand print_vector_float float_rot return_char_pop vector_string_contains
vector_boolean_occurrencesof genome_empty zip_prev genome_toggle_silent vector_string_reverse zip_dup code_cons code_number exec_stackdepth float_flush
boolean_and vector_boolean_boolean string_length float_con string_frominteger exec_flush vector_string_empty exec_show vector_float_swap genome_close_dec
code_insert vector_boolean_pop float_div zip_insert_right fromcode code_fromboolean vector_boolean_take code_show environment_begin vector_float_take
boolean_invert_second_then_and code_container code_nth vector_boolean_subvec float_yank zip_zip up vector_boolean_emptyvector vector_boolean_replacefirst
string_fromfloat vector_boolean_yankdup string_dup boolean_yankdup exec_fromziplefts
```

More

- Input instructions
- Print instructions
- Associative storage via tags
- Environment/return stacks
- Limits, termination modes

Clojush

Lee Spector (lspector@shampshire.edu), started 20100227 See version history. Older version history is in old-version-history.txt.

This is the README file accompanying Clojush, an implementation of the Push programming language and the PushGP genetic programming system in the Clojure programming language. Among other features this implementation takes advantage of Clojure's facilities for multi-core concurrency.

Availability

<https://github.com/lspector/Clojush/>

Requirements

To use this code you must have a Clojure programming environment; see <http://clojure.org/>. The current version of Clojush requires Clojure 1.7.0.

Clojure is available for most OS platforms. A good starting point for obtaining and using Clojure.

Quickstart

Using Leiningen you can run an example from the OS command line (in the Clojush directory) with a call like:

```
lein run clojush.problems.demos.simple-regression
```

```
;; https://github.com/lspector/Clojush/
```

```
=> (run-push '(1 2 integer_add) (make-push-state))
```

```
:exec ((1 2 integer_add))
:integer ( )
```

```
:exec (1 2 integer_add)
:integer ( )
```

```
:exec (2 integer_add)
:integer (1)
```

```
:exec (integer_add)
:integer (2 1)
```

```
:exec ( )
:integer (3)
```

```
=> (run-push '(2 3 integer_mult 4.1 5.2 float_add
               true false boolean_or)
      (make-push-state))
```

```
:exec ()
:integer (6)
:float (9.3)
:boolean (true)
```

In other words

- Put 2×3 on the integer stack
- Put $4.1 + 5.2$ on the float stack
- Put *true* ∨ *false* on the boolean stack

```
=> (run-push '(2 boolean_and 4.1 true integer_div
               false 3 5.2 boolean_or integer_mult
               float_add)
      (make-push-state))
```

```
:exec ()
:integer (6)
:float (9.3)
:boolean (true)
```

Same as before, but

- Several operations (e.g., *boolean_and*) become NOOPs
- Interleaved operations

```
=> (run-push
      '(4.0 exec_dup (3.13 float_mult) 10.0 float_div)
      (make-push-state))
```

```
:exec ((4.0 exec_dup (3.13 float_mult) 10.0 float_div))
:float ()
```

```
:exec (4.0 exec_dup (3.13 float_mult) 10.0 float_div)
:float ()
```

```
:exec (exec_dup (3.13 float_mult) 10.0 float_div)
:float (4.0)
```

```
:exec((3.13 float_mult) (3.13 float_mult) 10.0 float_div)
:float (4.0)
```

...

```
:exec ()
:float (3.91876)
```

Computes $4.0 \times 3.13 \times 3.13 / 10.0$

```
=> (run-push '(1 8 exec_do*range integer_mult)
      (make-push-state))
```

```
:integer (40320)
```

Computes $8!$ in a fairly “human” way


```
=> (run-push '(code_quote
  (code_quote (integer_pop 1)
    code_quote (code_dup integer_dup
      1 integer_sub code_do
        integer_mult)
      integer_dup 2 integer_lt code_if)
    code_dup
      8
    code_do)
  (make-push-state)))

:code ((code_quote (integer_pop 1) code_quote (code_dup
  integer_dup 1 integer_sub code_do integer_mult)
  integer_dup 2 integer_lt code_if))
:integer (40320)
```

A less “obvious” recursive calculation of 8! achieved by code duplication

```
=> (run-push '(0 true exec_while
  (1 integer_add true))
  (make-push-state))

:exec (1 integer_add true exec_while (1 integer_add
  true))
:integer (199)
:termination :abnormal
```

- An infinite loop
- Terminated by eval limit
- Result taken from appropriate stack(s) upon termination

```
=> (run-push '(in1 in1 float_mult 3.141592 float_mult)
  (push-item 2.5 :input (make-push-state)))

:float (19.63495)
:input (2.5)
```

Computes the area of a circle with the given radius: $3.141592 \times in1 \times in1$

Genetic Programming

Linear Genomes

- Support uniform variation
- Structure where we want it, via translation
- ULTRA: Uniform Linear Transformation with Repair and Alternation
- PLUSH: epigenetic markers (Clojush)
- Plushy: close instructions (plushi, propel)

Uniform Variation

- All genetic material that a child inherits should be $\approx$ likely to be mutated
- Parts of both parents should be $\approx$ likely to appear in children (at least if they are $\approx$ in size), and to appear in a range of combinations
- Should be applicable to genomes of varying size and structure

Structure

- Parentheses matter mostly for defining code blocks for **exec** instructions
- Openings of blocks can be determined by placement of relevant **exec** instructions
- Closings of blocks can be encoded in genomes in several ways

ULTRA

- Linearize just during variation:
 - Linearize two parents
 - Alternate according to *alternation rate*, subject to *alignment deviation*
 - Uniformly mutate, subject to *mutation rate*
 - Repair
- Uniform, but structure anywhere

Plush

Instruction	integer_eq	exec_dup	char_swap	integer_add	exec_if	
Close?	2	0	0	0	1	
Silence?	1	0	0	1	0	

- Linear sequences of instructions and literals
- Instructions specify opens; epigenetic markers specify closes
- Permits uniform linear genetic operators
- Facilitates useful placement of code blocks
- Allows for epigenetic hill-climbing

Plushy

- Instructions specify opens
- "close" pseudo-instructions specify closes
- Used in plushi, propel

Genetic Operators

- Uniform mutation
- Alternation
- Uniform crossover
- Uniform mutation by addition and deletion (UMAD)
- Autoconstruction (genome instructions)

PushGP in Clojush

Set up run for target $x^3 - 2x^2 - x$

```
(pushgp
  {:error-function
   (fn [{:keys [program] :as individual}]
     (assoc individual :errors
              (vec
               (for [input (mapv float (range 10))]
                 (let [output (-> (make-push-state)
                                   (push-item input :input)
                                   (run-push program)
                                   (top-item :float))]
                   (if (number? output)
                     (Math/abs (float (- output
                                           (- (* input input input)
                                              (* 2 input input)
                                              input))))
                     1000000))))))
   :atom-generators
   '(in1 float_div float_mult float_add float_sub))}
```

DEMO

Problems Solved by PushGP in the GECCO-2005 Paper on Push3

- Reversing a list
- Factorial (many algorithms)
- Fibonacci (many algorithms)
- Parity (any size input)
- Exponentiation
- Sorting

Figure 8.7. A gate array diagram for an evolved version of Grover's database search algorithm for a 4-item database. The full gate array is shown at the top, with M_1 and M_2 standing for the smaller gate arrays shown at the bottom. A diagonal line through a gate symbol indicates that the matrix for the gate is transposed. The "f" gate is the oracle.

**Humies 2004
GOLD MEDAL**

Genetic Programming for Finite Algebras

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**Humies 2008
GOLD MEDAL**

29 Software Synthesis Benchmarks

- Number IO, Small or Large, For Loop Index, Compare String Lengths, Double Letters, [Collatz Numbers](#), Replace Space with Newline, String Differences, Even Squares, [Wallis Pi](#), String Lengths Backwards, Last Index of Zero, Vector Average, Count Odds, Mirror Image, [Super Anagrams](#), Sum of Squares, Vectors Summed, X-Word Lines, [Pig Latin](#), Negative to Zero, Scrabble Score, [Word Stats](#), Checksum, Digits, Grade, Median, Smallest, Syllables
- PushGP has solved all of these except for the ones in [blue](#)
- Presented in a GECCO-2015 GP track paper

Auto-Simplification

- Loop:
 - Make it randomly simpler
 - Keep simpler if as good or better; otherwise revert
- GECCO-2014 poster: efficiently and reliably reduces the size of the evolved programs
- GECCO-2014 student paper: used as genetic operator
- GECCO-2017 GP best paper nominee: improves generalization

SUCCESS at generation 20

[illegible][illegible]

Auto-simplifying with starting size: 231

...

step: 5000

```
program: (\space \newline in1 string_replacechar print_string "Wx{ "  
string_last in1 string_removechar string_length)
```

[illegible]

```

Total error: 0.0

```

```
Size: 11
```

Checksum

Multiple types, looping, and code blocks

Simplified solution:

```

("Check sum is " print_string
 in1 64 exec_string_iterate (integer_fromchar integer_add)
 64 integer_mod
 \space integer_fromchar integer_add char_frominteger
 print char)

```

Checksum

Multiple types, looping, and code blocks

Simplified solution:

```
("Check sum is " print_string
  inl 64 exec_string_iterate (integer_fromchar integer_add)
  64 integer_mod
  \space integer_fromchar integer_add char_frominteger
  print_char)
```

First: Print out the header

Checksum

Multiple types, looping, and code blocks

Simplified solution:

```
("Check sum is " print_string
  inl 64 exec_string_iterate (integer_fromchar integer_add)
  64 integer_mod
  \space integer_fromchar integer_add char_frominteger
  print_char)
```

Second: Convert each character to an integer, sum,
and add to 64.

Checksum

Multiple types, looping, and code blocks

Simplified solution:

```
("Check sum is " print_string
  inl 64 exec_string_iterate (integer_fromchar integer_add)
  64 integer_mod
  \space integer_fromchar integer_add char_frominteger
  print_char)
```

Third: Mod result by 64

Checksum

Multiple types, looping, and code blocks

Simplified solution:

```
("Check sum is " print_string
  inl 64 exec_string_iterate (integer_fromchar integer_add)
  64 integer_mod
  \space integer_fromchar integer add char frominteger
  print_char)
```

Third: Add modulus result to 32 and convert to char

Checksum

Multiple types, looping, and code blocks

Simplified solution:

```
("Check sum is " print_string
 inl 64 exec_string_iterate (integer_fromchar integer_add)
 64 integer_mod
 \space integer_fromchar integer_add char_frominteger
 print_char)
```

Fourth: Print resulting char

Replace Space With Newline

Multiple types, looping, multiple tasks

Simplified solution:

```
(\space char_dup exec_dup inl
 \newline string_replacechar print_string
 string_removechar string_length)
```

Replace Space With Newline

Multiple types, looping, multiple tasks

Simplified solution:

```
(\space char_dup exec_dup inl
 \newline string_replacechar print_string
 string_removechar string_length)
```

First: Duplicate space character and input string for use in both tasks

Replace Space With Newline

Multiple types, looping, multiple tasks

Simplified solution:

```
(\space char_dup exec_dup inl
 \newline string_replacechar print_string
 string_removechar string_length)
```

Second: Replace spaces with newlines and print

Replace Space With Newline

Multiple types, looping, multiple tasks

Simplified solution:

```
(\space char_dup exec_dup inl  
 \newline string_replacechar print_string  
 string_removechar string_length)
```

Third: Remove all spaces from second copy of input,
and push length of result on integer stack for return

DEMO

Variation in GP

Variation in GP

Autoconstruction

Autoconstruction

A bit more complicated when genomes distinguished from programs

Autoconstruction

- Evolve evolution while evolving solutions
- How? Individuals produce and vary their own children, with methods that are subject to variation
- Requires understanding the evolution of variation
- Hope: May produce EC systems more powerful than we can write by hand

Autoconstruction

- A 15 year old project (building on older and broader-based ideas)
- Like genetic programming, but harder and less successful! But with greater potential?
- Recent versions sometimes solve significant problems, intriguing patterns of evolving evolution

For Evolution²

- Diversity: Individuals vary
- Diversification: Individuals produce descendants that vary, in various ways
- Recursive Variance: Individuals produce descendants that vary in the ways that they vary their offspring

Figure 1: DL-distances between parent and child during a single non-autoconstructive run of GP on the Replace Space With Newline problem

Figure 3: DL-distances between parent and child during a single autoconstructive run of GP on the Replace Space With Newline problem

Evolution Evolving

- Autoconstructive evolution can sometimes succeed as much and as fast as non-autoconstructive evolution
- Autoconstruction found solutions for the string differences software synthesis problem before ordinary GP

Conclusions

- Push supports evolution of expressive programs that use arbitrary types and control structures, possibly to perform multiple tasks
- Push interpreters, and GP systems that evolve Push programs, are easy to write
- Push supports research on expressiveness in genetic programming, for example to support the evolution of modularity

Thanks

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