Using Higher-Order Logic Programming for Semantic Interpretation of Coordinate Constructs

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Abstract

Many theories of semantic interpretation use λ -term manipulation to compositionally compute the meaning of a sentence. These theories are usually implemented in a language such as Prolog that can simulate λ -term operations with first-order unification. However, for some interesting cases, such as a Combinatory Categorical Grammar account of coordination constructs, this can only be done by obscuring the underlying linguistic theory with the “tricks” needed for implementation. This paper shows how the use of abstract syntax permitted by higher-order logic programming allows an elegant implementation of the semantics of Combinatory Categorical Grammar, including its handling of coordination constructs.

1 Introduction

Many theories of semantic interpretation use λ -term manipulation to compositionally compute the meaning of a sentence. These theories are usually implemented in a language such as Prolog that can simulate λ -term operations with first-order unification. However, there are cases in which this can only be done by obscuring the underlying linguistic theory with the “tricks” needed for implementation. For example, Combinatory Categorical Grammar (CCG) (Steedman, 1990) is a theory of syntax and semantic interpretation that has the attractive characteristic of handling many coordination constructs that other theories cannot. While many aspects of CCG semantics can be reasonably simulated in first-order unification, the simulation breaks down on some of the most interesting cases that CCG can theoretically handle. The problem in general, and for CCG in particular, is that the implementation language does not have sufficient expressive power to allow a more direct encoding. The solution given in this paper is to show how advances in logic programming allow the implementation of semantic theories in a

very direct and natural way, using CCG as a case study.

We begin by briefly illustrating why first-order unification is inadequate for some coordination constructs, and then review two proposed solutions. The sentence in (1a) usually has the logical form (LF) in (1b).

(1a) John and Bill run.

(1b) (and (run John) (run Bill))

CCG is one of several theories in which (1b) gets derived by raising *John* to be the LF $\lambda P.(P \text{ john})$, where P is a predicate that takes a NP as an argument to return a sentence. Likewise, *Bill* gets the LF $\lambda P.(P \text{ bill})$, and coordination results in the following LF for *John and Bill*:

(2) $\lambda P.(\text{and } (P \text{ john}) (P \text{ bill}))$

When (2) is applied to the predicate, (1b) will result after β -reduction. However, under first-order unification, this needs to be simulated by having the variable x in $\lambda x.\text{run}(x)$ unify both with Bill and John, and this is not possible. See (Jowsey, 1990) and (Moore, 1989) for a thorough discussion.

(Moore, 1989) suggests that the way to overcome this problem is to use explicit λ -terms and encode β -reduction to perform the needed reduction. For example, the logical form in (3) would be produced, where $\mathbf{X}\backslash\text{run}(\mathbf{X})$ is the representation of $\lambda x.\text{run}(x)$.

(3) and(apply($\mathbf{X}\backslash\text{run}(\mathbf{X})$, john),

apply($\mathbf{X}\backslash\text{run}(\mathbf{X})$, bill))

This would then be reduced by the clauses for *apply* to result in (1b). For this small example, writing such an *apply* predicate is not difficult. However, as the semantic terms become more complex, it is no trivial matter to write β -reduction that will correctly handle variable capture. Also, if at some point it was desired to determine if the semantic forms of two different sentences were the same, a predicate would be needed to compare two lambda forms for α -equivalence, which again is not a simple task. Essentially, the logic variable $\mathbf{X}$ is meant to be interpreted as a bound variable, which requires an additional layer of programming.

(Park, 1992) proposes a solution within first-order unification that can handle not only sentence (1a), but also more complex examples with determiners. The method used is to introduce spurious bindings that subsequently get removed. For example, the semantics of (4a) would be (4b), which would then get simplified to (4c).

- (4a) A farmer and every senator talk
- (4b) `exists(X1,farmer(X1)`
`&(exists(X2,(X2=X1)&talk(X2)))`
`&forall(X3,senator(X3)`
`=>(exists(X2,(X2=X3)&talk(X2))))`
- (4c) `exists(X1,farmer(X1)&talk(X1))`
`&forall(X3,senator(X3)=>talk(X3))`

While this pushes first-order unification beyond what it had been previously shown capable of, there are two disadvantages to this technique: (1) For every possible category that can be conjoined, a separate lexical entry for *and* is required, and (2) As the conjoinable categories become more complex, the *and* entries become correspondingly more complex and greatly obscure the theoretical background of the grammar formalism.

The fundamental problem in both cases is that the concept of free and bound occurrences of variables is not supported by Prolog, but instead needs to be implemented by additional programming. While theoretically possible, it becomes quite problematic to actually implement. The solution given in this paper is to use a higher-order logic programming language, λ Prolog, that already implements these concepts, called “abstract syntax” in (Miller, 1991) and “higher-order abstract syntax” in (Pfenning and Elliot, 1988). This allows a natural and elegant implementation of the grammatical theory, with only one lexical entry for *and*. This paper is meant to be viewed as furthering the exploration of the utility of higher-order logic programming for computational linguistics - see, for example, (Miller & Nadathur, 1986), (Pareschi, 1989), and (Pereira, 1990).

2 CCG

CCG is a grammatical formalism in which there is a one-to-one correspondence between the rules of composition¹ at the level of syntax and logical form. Each word is (perhaps ambiguously) assigned a category and LF, and when the syntactical operations assign a new category to a constituent, the corresponding semantic operations produce a new LF for that constituent as well. The CCG rules shown in Figure 1 are implemented in the system described

¹In the general sense, not specifically the CCG rule for function composition.

Function Application ($>$):
 $X/Y : F \quad Y : y \Rightarrow X : Fy$

Function Application ($<$):
 $Y : y \quad X \backslash Y : F \Rightarrow X : Fy$

Function Composition ($> B$):
 $X/Y : F \quad Y/Z : G \Rightarrow X/Z : \lambda x.F(Gx)$

Function Composition ($< B$):
 $Y \backslash Z : G \quad X \backslash Y : F \Rightarrow X \backslash Z : \lambda x.F(Gx)$

Type Raising ($> T$):
 $np : x \Rightarrow s/(s \backslash np) : \lambda F.Fx$

Type Raising ($< T$):
 $np : x \Rightarrow s \backslash (s/np) : \lambda F.Fx$

Figure 1: CCG rules

harry	found
----->T -----	
S:s/(S:s\NP:harry')	
(S:found' np1 np2\NP:np1)/NP:np2	
----->B -----	
S:found' harry' np2/NP:np2	

Figure 2: CCG derivation of *harry found* simulated by first-order unification

in this paper.^{2 3} Each of the three operations have both a forward and backward variant.

As an illustration of how the semantic rules can be simulated in first-order unification, consider the derivation of the constituent *harry found*, where *harry* has the category *np* with LF *harry'* and *found* is a transitive verb of category $(s \backslash np)/np$ with LF

(5) $\lambda object. \lambda subject. (found' subject object)$

In the CCG formalism, the derivation is as follows: *harry* gets raised with the $> T$ rule, and then forward composed by the $> B$ rule with *found*, and the result is a category of type s/np with LF $\lambda x.(found' harry' x)$. In section 3 it will be seen how the use of abstract syntax allows this to be expressed directly. In first-order unification, it is simulated as shown in Figure 2.⁴

The final CCG rule to be considered is the coordination rule that specifies that only like categories can coordinate:

²The type-raising rules shown are actually a simplification of what has been implemented. In order to handle determiners, a system similar to NP-complement categories as discussed in (Dowty, 1988) is used. Although a worthwhile further demonstration of the use of abstract syntax, it has been left out of this paper for space reasons.

³The $\backslash$ for a backward-looking category should not be confused with the $\backslash$ for λ -abstraction.

⁴example adapted from (Steedman, 1990, p. 220).

(6) $X \text{ conj } X \Rightarrow X$

This is actually a schema for a family of rules, collectively called “generalized coordination”, since the semantic rule is different for each case.⁵ For example, if X is a unary function, then the semantic rule is (7a), and if the functions have two arguments, then the rule is (7b).⁶

(7a) $\Phi FGH = \lambda x.F(Gx)(Hx)$

(7b) $\Phi^2 FGH = \lambda x.\lambda y.F(Gxy)(Hxy)$

For example, when processing (1a), rule (7a) would be used with:

- $F = \lambda x.\lambda y.(\text{and}' x y)$
- $G = \lambda P.(P \text{ john}')$
- $H = \lambda P.(P \text{ bill}')$

with the result

$$\phi FGH = \lambda x.(\text{and}' (x \text{ john}') (x \text{ bill}'))$$

which is α -equivalent to (2).

3 λ PROLOG and Abstract Syntax

λ Prolog is a logic programming language based on *higher-order hereditary Harrop formulae* (Miller et al., 1991). It differs from Prolog in that first-order terms and unification are replaced with simply-typed λ -terms and higher-order unification⁷, respectively. It also permits universal quantification and implication in the goals of clauses. The crucial aspect for this paper is that together these features permits the usage of abstract syntax to express the logical forms terms computed by CCG. The built-in λ -term manipulation is used as a “meta-language” in which the “object-language” of CCG logical forms is expressed, and variables in the object-language are mapped to variables in the meta-language.

The λ Prolog code fragment shown in Figure 3 declares how the CCG logical forms are represented. Each CCG LF is represented as an untyped λ -term, namely type **tm**. **abs** represents object-level abstraction $\lambda x.M$ by the meta-level expression (**abs** **N**),

⁵It is not established if this schema should actually produce an unbounded family of rules. See (Weir, 1988) and (Weir and Joshi, 1988) for a discussion of the implications for automata-theoretic power of generalized coordination and composition, and (Gazdar, 1988) for linguistic arguments that languages like Dutch may require this power, and (Steedman, 1990) for some further discussion of the issue. In this paper we use the generalized rule to illustrate the elegance of the representation, but it is an easy change to implement a bounded coordination rule.

⁶The Φ notation is used because of the combinatory logic background of CCG. See (Steedman, 1990) for details.

⁷defined as the unification of simply typed λ -terms, modulo $\beta\eta$ conversion.

kind	tm	type.
type	abs	$(\text{tm} \rightarrow \text{tm}) \rightarrow \text{tm}.$
type	app	$\text{tm} \rightarrow \text{tm} \rightarrow \text{tm}.$
type	forall	$(\text{tm} \rightarrow \text{tm}) \rightarrow \text{tm}.$
type	exists	$(\text{tm} \rightarrow \text{tm}) \rightarrow \text{tm}.$
type	>>	$\text{tm} \rightarrow \text{tm} \rightarrow \text{tm}.$
type	&&	$\text{tm} \rightarrow \text{tm} \rightarrow \text{tm}.$

Figure 3: Declarations for λ Prolog representation of CCG logical forms

where N is a meta-level function of type $\text{tm} \rightarrow \text{tm}$. A meta-level λ -abstraction $\lambda y.P$ is written $y \backslash P$.⁸

Thus, if **walked'** has type $\text{tm} \rightarrow \text{tm}$, then $y \backslash (\text{walked}' y)$ is a λ Prolog (meta-level) function with type $\text{tm} \rightarrow \text{tm}$, and (**abs** $y \backslash (\text{walked}' y)$) is the object-level representation, with type **tm**. The LF for *found* shown in (5) would be represented as (**abs** **obj** \ (**abs** **sub** \ (**found'** **sub** **obj**))). **app** encodes application, and so in the derivation of *harry found*, the type-raised *harry* has the λ Prolog value (**abs** **p** \ (**app** **p** *harry'*)).⁹

The second part of Figure 3 shows declares how quantifiers are represented, which are required since the sentences to be processed may have determiners. **forall** and **exists** are encoded similarly to abstraction, in that they take a functional argument and so object-level binding of variables by quantifiers is handled by meta-level λ -abstraction. **>>** and **&&** are simple constructors for implication and conjunction, to be used with **forall** and **exists** respectively, in the typical manner (Pereira and Shieber, 1987). For example, the sentence *every man found a bone* has as a possible LF (8a), with the λ Prolog representation (8b)¹⁰:

⁸This is the same syntax for λ -abstraction as in (3). (Moore, 1989) in fact borrows the notation for λ -abstraction from λ Prolog. The difference, of course, is that here the abstraction is a meta-level, built-in construct, while in (3) the interpretation is dependent on an extra layer of programming. Bound variables in λ Prolog can be either upper or lower case, since they are not logic variables, and will be written in lower case in this paper.

⁹It is possible to represent the logical forms at the object-level without using **abs** and **app**, so that *harry* could be simply **p** \ (**p** *harry'*). The original implementation of this system was in fact done in this manner. Space prohibits a full explanation, but essentially the fact that λ Prolog is a typed language leads to a good deal of formal clutter if this method is used.

¹⁰The LF for the determiner has the form of a Montagovian generalized quantifier, giving rise to one fully scoped logical form for the sentence. It should be stressed that this particular kind of LF is assumed here purely for the sake of illustration, to make the point that composition at the level of derivation and LF are one-to-one. Section 4 contains an example for which such a

```

type apply  tm -> tm -> tm -> o.
type compose tm -> tm -> tm -> o.
type raise  tm -> tm -> o.

apply  (abs R) S (R S).
compose (abs F) (abs G) (abs x\ (F (G x))).
raise  Tm (abs P\ (app P Tm)).

```

Figure 4: λProlog implementation of CCG logical form operations

(8a) $\exists x.((\text{bone}' x) \wedge \forall y.((\text{man}' y) \rightarrow (\text{found}' y x)))$
(8b) `(exists x\
((bone' x) &&
(forall x1\
((man' x1) >> (found' x1 x))))`

Figure 4 illustrates how directly the CCG operations can be encoded¹¹. *o* is the type of a meta-level proposition, and so the intended usage of `apply` is to take three arguments of type *tm*, where the first should be an object-level λ-abstraction, and set the third equal to the application of the first to the second. Thus, for the query

```
?- apply (abs sub\ (walked' sub)) harry' M.
```

R unifies with the *tm* → *tm* function `sub\ (walked' sub)`, *S* with `harry'` and *M* with `(R S)`, the meta-level application of *R* to *S*, which by the built-in β-reduction is `(walked' harry')`. In other words, object-level function application is handled simply by the meta-level function application.

Function composition is similar. Consider again the derivation of *harry found* by type-raising and forward composition. *harry* would get type-raised by the `raise` clause to produce `(abs p\ (app p harry'))`, and then composed with *found*, with the result shown in the following query:

```
?- compose (abs p\ (app p harry'))
  (abs obj\  

    (abs sub\  

      (found' sub obj)))
  M.
M = (abs x\  

  (app  

    (abs sub\ (found' sub x))  

    harry')).
```

derivation fails to yield all available quantifier scopings. We do not address here the further question of how the remaining scoped readings are derived. Alternatives that appear compatible with the present approach are quantifier movement (Hobbs & Shieber, 1987), type-raising at LF (Partee & Rooth, 1983), or the use of disambiguated quantifiers in the derivation itself (Park, 1995).

¹¹There are other clauses, not shown here, that determine the direction of the CCG rule. For either direction, however, the semantics are the same and both directional rules call these clauses for the semantic computation.

```

kind  cat      type.
type  fs       cat -> cat -> cat.
type  bs       cat -> cat -> cat.

type  np       cat.
type  s        cat.
type  conj     cat.
type  noun     cat.

type  atomic-type  cat -> o.

atomic-type np.
atomic-type s.
atomic-type conj.
atomic-type noun.

```

Figure 5: Implementation of the CCG category system

At this point a further β-reduction is needed. Note however this is not at all the same problem of writing a β-reducer in Prolog. Instead it is a simple matter of using the meta-level β-reduction to eliminate β-redexes to produce the final result `(abs x\ (found' harry x))`. We won't show the complete declaration of the β-reducer, but the key clause is simply:

```
red (app (abs M) N) (M N).
```

Thus, using the abstract syntax capabilities of λProlog, we can have a direct implementation of the underlying linguistic formalism, in stark contrast to the first-order simulation shown in Figure 2.

4 Implementation of Coordination

A primary goal of abstract-syntax is to support recursion through abstractions with bound variables. This leads to the interpretation of a bound variable as a “scoped constant” - it acts like a constant that is not visible from the top of the term, but which becomes visible during the descent through the abstraction. See (Miller, 1991) for a discussion of how this may be used for evaluation of functional programs by “pushing” the evaluation through abstractions to reduce redexes that are not at the top-level. This technique is also used in the β-reducer briefly mentioned at the end of the previous section, and a similar technique will be used here to implement coordination by recursively descending through the two arguments to be coordinated.

Before describing the implementation of coordination, it is first necessary to mention how CCG categories are represented in the λProlog code. As shown in Figure 5, *cat* is declared to be a primitive type, and *np*, *s*, *conj*, *noun* are the categories used in this implementation. *fs* and *bs* are declared

```

type    coord
      cat -> tm -> tm -> tm -> o.

coord (fs A B) (abs R) (abs S) (abs T) :-
  pi x\ (coord B (R x) (S x) (T x)).

coord (bs A B) (abs R) (abs S) (abs T) :-
  pi x\ (coord B (R x) (S x) (T x)).

coord B R S (and' R S) :- atomic-type B.

```

Figure 6: Implementation of coordination

to be constructors for forward and backward slash. For example, the CCG category for a transitive verb ($s\backslash np$)/ np would be represented as $(fs\ np\ (bs\ np\ s))$. Also, the predicate `atomic-type` is declared to be true for the four atomic categories. This will be used in the implementation of coordination as a test for termination of the recursion.

The implementation of coordination crucially uses the capability of λ Prolog for universal quantification in the goal of a clause. `pi` is the meta-level operator for $\forall$, and $\forall x.M$ is written as `pi x\M`. The operational semantics for λ Prolog state that `pi x\G` is provable if and only if $[c/x]G$ is provable, where c is a new variable of the same type as x that does not otherwise occur in the current signature. In other words, c is a scoped constant and the current signature gets expanded with c for the proof of $[c/x]G$. Since c is meant to be treated as a generic placeholder for any arbitrary x of the proper type, c must not appear in any terms instantiated for logic variables during the proof of $[c/x]G$. The significance of this restriction will be illustrated shortly.

The code for coordination is shown in Figure 6. The four arguments to `coord` are a category and three terms that are the object-level LF representations of constituents of that category. The last argument will result from the coordination of the second and third arguments. Consider again the earlier problematic example (1a) of coordination. Recall that after *john* is type-raised, its LF will be $(abs\ p\ (app\ p\ john'))$ and similarly for *bill*. They will both have the category $(fs\ (bs\ np\ s))$. Thus, to obtain the LF for *John and Bill*, the following query would be made:

```

?- coord (fs (bs np s) s)
      (abs p\ (app p john'))
      (abs p\ (app p bill'))
      M.

```

This will match with the first clause for `coord`, with

- A instantiated to $(bs\ np\ s)$
- B to s
- R to $(p\ (app\ p\ john'))$
- S to $(p\ (app\ p\ bill'))$

- and T a logic variable waiting instantiation.

Then, after the meta-level β -reduction using the new scoped constant c , the following goal is called:

```

?- coord s (app c john') (app c bill') M.

```

where $M = (T\ c)$. Since s is an atomic type, the third `coord` clause matches with

- B instantiated to s
- R to $(app\ c\ john')$
- S to $(app\ c\ bill')$
- M to $(and' (app\ c\ john') (app\ c\ bill'))$

Since $M = (T\ c)$, higher-order unification is used by λ Prolog to instantiate T by extracting c from M with the result

```

T = x\ (and' (app x john') (app x bill'))

```

and so M from the original query is

```

(abs x\ (and' (app x john') (app x bill')))

```

Note that since c is a scoped constant arising from the proof of an universal quantification, the instantiation

```

T = x\ (and' (app c john') (app x bill'))

```

is prohibited, along with the other extractions that do not remove c from the body of the abstraction.

This use of universal quantification to extract out c from a term containing c in this case gives the same result as a direct implementation of the rule for coordination of unary functions (7a) would. However, this same process of recursive descent via scoped constants will work for any member of the `conj` rule family. For example, the following query

```

?- coord
      (fs np (bs np s))
      (abs obj\ (abs sub\ (like' sub obj)))
      (abs obj\ (abs sub\ (hate' sub obj)))
      M.
M = (abs x\
      (abs x1\
        (and' (like' x1 x)
              (hate' x1 x)))).

```

corresponds to rule (7b). Note also that the use of the same bound variable names `obj` and `sub` causes no difficulty since the use of scoped-constants, meta-level β -reduction, and higher-order unification is used to access and manipulate the inner terms. Also, whereas (Park, 1992) requires careful consideration of handling of determiners with coordination, here such sentences are handled just like any others. For example, the sentence *Mary gave every dog a bone and some policeman a flower* results in the LF 12.

¹²This is a case in which the particular LF assumed here fails to yield another available scoping. See footnote 10.

```
(and'
  (exists x\(((bone' x) &&
    (forall x1\((dog' x1)
      >> (gave' mary' x x1))))))
  (exists x\((flower' x) &&
    (exists x1\((policeman' x1)
      && (gave' mary' x x1))))))
```

Thus, “generalized coordination”, instead of being a family of separate rules, can be expressed as a single rule on recursive descent through logical forms. (Steedman, 1990) also discusses “generalized composition”, and it may well be that a similar implementation is possible for that family of rules as well.

5 Conclusion

We have shown how higher-order logic programming can be used to elegantly implement the semantic theory of CCG, including the previously difficult case of its handling of coordination constructs. The techniques used here should allow similar advantages for a variety of such theories.

An argument can be made that the approach taken here relies on a formalism that entails implementation issues that are more difficult than for the other solutions and inherently not as efficient. However, the implementation issues, although more complex, are also well-understood and it can be expected that future work will bring further improvements. For example, it is a straightforward matter to transform the λProlog code into a logic called L_λ (Miller, 1990) which requires only a restricted form of unification that is decidable in linear time and space. Also, the declarative nature of λProlog programs opens up the possibility for applications of program transformations such as partial evaluation.

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